

Suppose the true data generating process in the examples below are of the form

$$y_i = \beta_0 + \beta_1 x_i + \beta_2 o_i + u_i,$$

where  $x_i$  and  $o_i$  are exogenous such that  $\mathbb{E}[u_i|o, x] = 0$ .

However,  $o$  is a variable that cannot be observed and so instead, we run the model:

$$y_i = \beta_0 + \beta_1 x_i + \varepsilon_i \text{ where } \varepsilon_i = \beta_2 o_i + u_i$$

Recall that we can sign the bias by:

$$\mathbb{E}[\hat{\beta}_1] = \beta_1 + \beta_2 \frac{\text{Cov}(X_i, Z_i)}{\text{Var}(X_i)}$$

### Causal Effect of Migration on Earnings

1. Suppose we took survey data that included people's earnings and whether they have recently moved to a new city or not, and we estimated this model:

$$\text{Earnings}_i = \beta_0 + \beta_1 \text{Migration}_i + \varepsilon_i$$

Consider the unobservable variable absorbed in  $\varepsilon_i$  which is  $o_i = \text{ambition}_i$ .

- (a) How does *Ambition* correlate with *Earnings*? That is, would you expect  $\beta_2$  to be positive, negative or 0?
- (b) How does *Ambition* correlate with *Migration*? That is, would you expect  $\text{Cov}(\text{migration}, \text{ambition})$  to be positive, negative or 0?
- (c) We have to omit *ambition* from the model because it is not observable. Considering your answers to parts (a) and (b), we should expect that  $\hat{\beta}_1$  will be biased (circle one):  
up / down / not at all.

**Causal Effect of Friends of the Opposite Sex on a High School Student's GPA**

2. Suppose we took survey data that included high school student's GPAs and the number of friends of the opposite sex they have, and we estimated the following model:

$$GPA_i = \beta_0 + \beta_1 \text{Opposite Sex Friends}_i + \varepsilon_i$$

Consider the unobservable variable absorbed in  $\varepsilon_i$  which is  $o_i = \text{strict parents}_i$ .

- (a) How does *Strict Parents* correlate with *GPA*? That is, would you expect  $\beta_2$  to be positive, negative or 0?
- (b) How does *Strict Parents* correlate with *Opposite Sex Friends*? That is, would you expect  $Cov(\text{Opposite Sex Friends}, \text{Strict Parents})$  to be positive, negative, or 0?
- (c) We have to omit *Strict Parents* from the model because it is not observable. Considering your answers to parts (a) and (b), we should expect that  $\hat{\beta}_1$  will be biased (circle one):  
up / down / not at all.

3. For the questions below, suppose you estimate the following model:

$$weight = 0 - 140 \cdot female + 30 \cdot height + 20 \cdot height \times female + u$$

- (a) How much would you predict a 6 foot male weighs?
  
  
  
  
  
  
  
  
  
  
- (b) How much would you predict a 6 foot female weighs?
  
  
  
  
  
  
  
  
  
  
- (c) What is the estimated impact of a one-unit (one foot) increase in height for a male individual?
  
  
  
  
  
  
  
  
  
  
- (d) What is the estimated impact of a one-unit (one foot) increase in height for a female person?
  
  
  
  
  
  
  
  
  
  
- (e) Which group has the steeper slope when it comes to how height ( $x$ ) impacts weight ( $y$ )?